

**TARTU UNIVERSITY**



**DOUBLE LAYER AND ADSORPTION  
AT SOLID ELECTRODES**

**IX**

**Tartu 1991**

GENERATION OF VARIABLE SIGN SPACE CHARGE IN A DIFFUSION LAYER FOR ELECTRODE PROCESS WITH SUBSEQUENT HOMOGENEOUS REACTION

Yu.I.Kharkats, A.V.Sokirko

A.N.Frumkin Institute of Electrochemistry, USSR Acad.Sci., Moscow

It is known that during electric current passing, a space charge region arises in diffusion layer, whose distribution density does not decrease exponentially as it was in diffuse layer, but gradually [1]. When the current density tends to its limiting value, the space charge density in the vicinity of the electrode increases abruptly, coinciding in sign with that for electroactive ions.

Here we present the results of investigation of space charge distribution in diffusion layer for reduction of cations  $A^{z+} + 2e^- \rightarrow A^0$ , and parallel oxygen reduction  $O_2 + 2H_2O + 4e^- \rightarrow 4OH^-$  with subsequent recombination reaction of  $OH^-$  and  $H^+$  ions in diffusion layer:  $OH^- + H^+ \rightarrow H_2O$ . This reaction scheme was analyzed in detail in ref. [2], in which the mechanism of migration current exaltation effect in acidic solution was theoretically investigated.

The set of electrodiffusion equations describing the distribution of components' concentrations and the potential in diffusion layer may be written as

$$\frac{dc_1}{dx} + c_1 \frac{d\psi}{dx} = \frac{i_1 L}{FD_1 c_0}, \quad \frac{dc_2}{dx} - c_2 \frac{d\psi}{dx} = 0, \quad (1)$$

$$D_3 \frac{dc_3}{dx} - c_3 \frac{d\psi}{dx} - D_4 \frac{dc_4}{dx} + c_4 \frac{d\psi}{dx} = -\frac{i_2 L}{Fc_0} = -D_3 j_2, \quad (2)$$

$$c_3 c_4 = K_0, \quad c_2 + c_3 = c_1 + c_4. \quad (3)$$

Here  $c_1$ ,  $c_2$ ,  $c_3$  and  $c_4$  are dimensionless concentrations of cations  $A^+$ , anions,  $OH^-$  ions and  $H^+$  ions,  $c_0$  is the dimensional concentration of  $A^+$  ions in the solution bulk,  $\psi = F\phi/RT$  is the dimensionless electric potential,  $x$  is di-

meneionless coordinate ( $0 \leq x \leq 1$ ),  $L$  is the thickness of the Nernst diffusion layer,  $i_1$  and  $i_2$  are current densities for cation's discharge and oxygen reduction,  $K_0$  - the ionic product for water, the boundary conditions at  $x = 1$  can be written as  $c_1(1) = 1$ ,  $c_2(1) = 1 + k$ ,  $c_3(1) = 0$ ,  $c_4(1) = k$ ,  $\psi(1) = 0$ .

Taking into account that the recombination reaction for water is very fast and the equilibrium constant satisfies inequality  $K_0 \ll 1$ , we can suppose that in the diffusion layer either ions  $\text{OH}^-$  or  $\text{H}^+$  ions can exist simultaneously. Correspondingly, the recombination of reaction plane  $x=0$  splits the diffusion layer into two regions,  $0 \leq x \leq \theta$  and  $\theta \leq x \leq 1$ . We can put  $c_4 > 0$  and  $c_3 \approx 0$  in the region spaced to the right of the point  $x = \theta$  and  $c_3 > 0$  and  $c_4 \approx 0$  in the region spaced to the left of the point  $x = 0$ . These approximations make it possible to determine the potential distribution  $\psi(x)$  and then using the Poisson equation, to find space charge distribution  $\rho = -\epsilon RT\psi''/F$ .

Calculated  $\rho(x)$  distributions for series of parameters  $j_1$ , and fixed  $j_2$  and  $k$  values are shown in Figure 1.

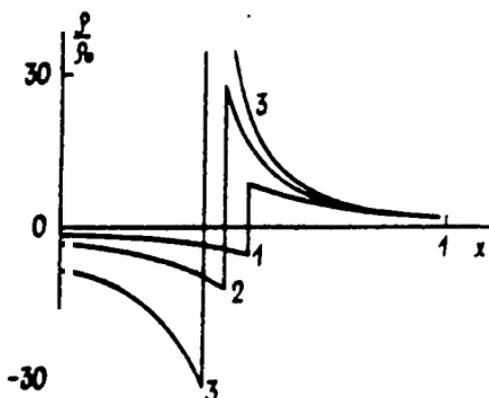


Fig. 1 Space charge distribution for  $D_3/D_4 = 0.56$ ;  $k = 0.8$ ;  $j_2 = 4$ , and  $j_1$ : 1 - 2; 2 - 2.5; 3 - 2.7;  $\phi_0 = 2 \text{ sec}^\circ$ .  $\cdot (l_D/L)^2$ ;  $l_D$  is the Debye length.

The analysis shows that as a result of recombination

reaction inside the diffusion layer some interesting peculiarities in space charge distribution arise. At the point of homogeneous reaction localization  $x = \theta$  and under the condition  $D_3 j_2 \ll D_4 j_1$ , an abrupt change of the sign and absolute value of  $\rho(x)$  takes place. In the discussed model due to high value of rate constant of recombination reaction its reaction layer had practically zero thickness. In a more general case of moderate reaction rates there must exist some transition region in which space charge varies from positive to negative values. Qualitatively the obtained result can be explained as follows. We can present the plane of recombination reaction localization as some electrode plane at  $x = \theta$ , which is on the one hand brought into contact with  $R^+$  ions, and on the other hand with  $OH^-$  ions. Then in the region  $\theta \leq x \leq 1$  where  $R^+$  ions exist we have positive space charge distribution as usual in electrolyte. And in the region  $0 \leq x \leq \theta$  where  $OH^-$  exists we have correspondingly negative space charge distribution.

We note in conclusion that the peak in space charge distributions including also a change in the sign of charge was earlier predicted in refs. /3,4/ for the systems in which besides movable carriers of charge also fixed charges exist.

#### References

1. V.G.Levich. Physico-chemical Hydrodynamics. M, 1959.
2. A.V.Sokirko, Yu. I.Kharkats, Elektrokhimiya.25 (1989) 232
3. Yu.I.Kharkats, Elektrokhimiya, 20 (1984) 248.
4. Yu.Ya.Gurevich, A.V.Noskov, Yu.I.Kharkats, Elektrokhimiya, Proc. Acad. Sci USSR, 298 (1988) 383.